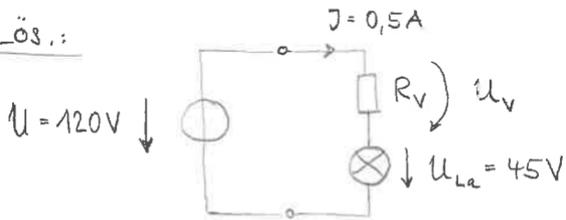


Aufgabe 2.1

Geg.: $U = 120\text{V}$; $U_{La} = 45\text{V}$; $J = 0,5\text{A}$;

Ges.: $R_V = ?$

Lös.:



$$U = U_V + U_{La}$$

$$U_V = U - U_{La} = 120\text{V} - 45\text{V} = 75\text{V};$$

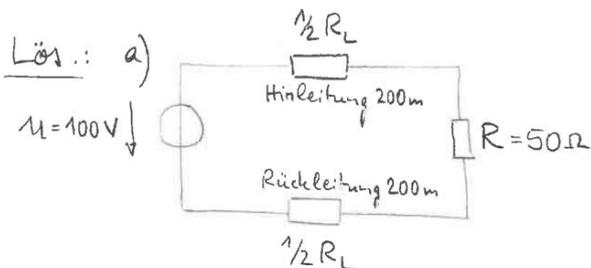
$$R_V = \frac{U_V}{J} = \frac{75\text{V}}{0,5\text{A}} = 150\Omega;$$

Aufgabe 2.2

Geg.: Leitungswiderstand R_L : $d = 1,5\text{mm}$; $l = 200\text{m}$ (bzw. $l = 400\text{m}$ für Hin- u. Rückleitung);
 $\epsilon_{Cu} = 0,018 \frac{\Omega \cdot \text{mm}^2}{\text{m}}$;

Verbraucherwiderstand $R = 50\Omega$;
 Quellenspannung $U = 100\text{V}$;

Ges.: a) Schaltung b) $R_L = ?$; $U_R = ?$; u_L in % = ?;



$$A = \frac{d^2 \cdot \pi}{4} = \frac{(1,5\text{mm})^2 \cdot \pi}{4} = 1,767\text{mm}^2;$$

b) $R_L = \frac{\epsilon_{Cu} \cdot l}{A} = \frac{0,018 \frac{\Omega \cdot \text{mm}^2}{\text{m}} \cdot 400\text{m}}{1,767\text{mm}^2} = 4,075\Omega;$

$$J = \frac{U}{R_L + R} = \frac{100\text{V}}{4,075 \frac{\text{V}}{\text{A}} + 50 \frac{\text{V}}{\text{A}}} = 1,850\text{A};$$

$$U_R = J \cdot R = 1,850\text{A} \cdot 50 \frac{\text{V}}{\text{A}} = 92,5\text{V};$$

$$U_L = U - U_R = 100\text{V} - 92,5\text{V} = 7,5\text{V};$$

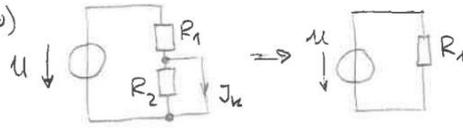
$$u_L = \frac{U_L}{U} \cdot 100\% = \frac{7,5\text{V}}{100\text{V}} \cdot 100\% = 7,5\%;$$

Aufgabe 2.3

Geg.: $U = 60V$; $U_2 = 10V$; $J_k = 1,0A$;

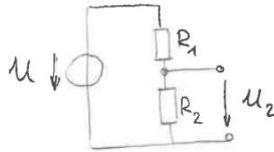
Ges.: R_1 und R_2

Lös.: aus Bild b)



$$R_1 = \frac{U}{J_k} = \frac{60V}{1,0A} = \underline{60\Omega}$$

Spannungsteilerregel:



$$\frac{U_2}{U} = \frac{R_2}{R_1 + R_2}$$

$$\frac{R_1 + R_2}{R_2} = \frac{U}{U_2} \quad \rightarrow$$

$$\frac{R_1}{R_2} + 1 = \frac{U}{U_2} \quad \rightarrow \quad \frac{R_1}{R_2} = \frac{U}{U_2} - 1 \quad \rightarrow \quad R_2 = \frac{R_1}{\frac{U}{U_2} - 1}$$

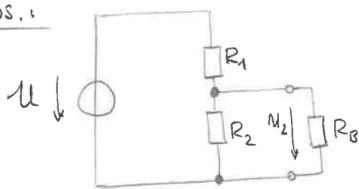
$$\rightarrow \underline{R_2} = \frac{R_1}{\frac{U}{U_2} - 1} = \frac{60\Omega}{\frac{60V}{10V} - 1} = \underline{12\Omega}$$

Aufgabe 2.4

Geg.: $U = 100V$; $R = R_1 + R_2 = 400\Omega$; $R_B = 800\Omega$; $U_2 = 40V$;

Ges.: R_1 und R_2

Lös.:



$$R_{2||B} = \frac{R_2 \cdot R_B}{R_2 + R_B}$$

Spannungsteilerregel: $\frac{U_2}{U} = \frac{R_{2||B}}{R_1 + R_{2||B}}$

$$\rightarrow U_2 = \frac{\frac{R_2 \cdot R_B}{R_2 + R_B}}{R_1 + \frac{R_2 \cdot R_B}{R_2 + R_B}} \cdot U = \frac{R_2 \cdot R_B}{R_1 \cdot R_2 + R_1 \cdot R_B + R_2 \cdot R_B}$$

mit $R_1 = R - R_2$: $U_2 = \frac{R_2 \cdot R_B}{(R - R_2) \cdot R_2 + (R - R_2) \cdot R_B + R_2 \cdot R_B} \cdot U$

$$\frac{R \cdot R_2 - R_2^2 + R \cdot R_B - R_2 \cdot R_B + R_2 \cdot R_B}{R_2 \cdot R_B} = \frac{U}{U_2}$$

$$-R_2^2 + R \cdot R_2 + R \cdot R_B = \frac{U}{U_2} \cdot R_B \cdot R_2$$

$$R_2^2 + \frac{U}{U_2} \cdot R_B \cdot R_2 - R \cdot R_2 - R \cdot R_B = 0$$

$$R_2^2 + \left(\frac{U}{U_2} \cdot R_B - R \right) \cdot R_2 - R \cdot R_B = 0$$

$$R_2^2 + \left(\frac{100V}{40V} \cdot 800\Omega - 400\Omega \right) \cdot R_2 - 400\Omega \cdot 800\Omega = 0$$

$$R_2^2 + 1600\Omega \cdot R_2 - 320000\Omega^2 = 0$$

$$ax^2 + bx + c = 0$$

$$x_{1/2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$R_2 = \frac{-1600\Omega \pm \sqrt{(1600\Omega)^2 + 4 \cdot 1 \cdot 320000\Omega^2}}{2 \cdot 1}$$

$$= \frac{-1600\Omega \pm \sqrt{3,84 \cdot 10^6 \Omega^2}}{2} = \frac{-1600\Omega \pm 1959,6\Omega}{2} = \underline{180\Omega};$$

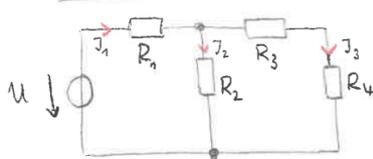
$$R_1 = R - R_2 = 400\Omega - 180\Omega = \underline{220\Omega};$$

Aufgabe 2.5

Ges.: $R_1 = 20\Omega$; $R_2 = 30\Omega$; $R_3 = 10\Omega$; $R_4 = 50\Omega$; $U = 12V$;

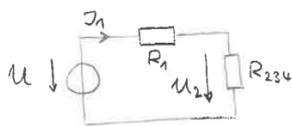
Ges.: J_1 , J_2 und J_3

Lös.:



$$R_2 \parallel R_3 + R_4$$

$$R_{234} = \frac{R_2 \cdot (R_3 + R_4)}{R_2 + R_3 + R_4} = \frac{30\Omega \cdot (10\Omega + 50\Omega)}{30\Omega + 10\Omega + 50\Omega} = \underline{20\Omega};$$



$$J_1 = \frac{U}{R_1 + R_{234}} = \frac{12V}{20\Omega + 20\Omega} = 0,3A = \underline{300mA};$$

$$U_2 = J_1 \cdot R_{234} = 0,3A \cdot 20\frac{V}{A} = \underline{6,0V};$$

$$J_2 = \frac{U_2}{R_2} = \frac{6,0V}{30\frac{V}{A}} = 0,2A = \underline{200mA};$$

$$J_1 = J_2 + J_3$$

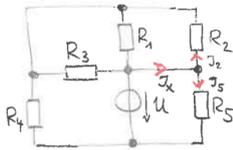
$$\rightarrow J_3 = J_1 - J_2 = 0,3A - 0,2A = 0,1A = \underline{100mA};$$

Aufgabe 2.6

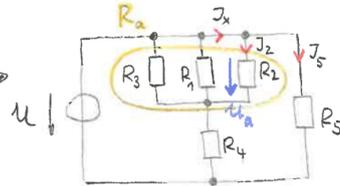
Geg.: $R_1 = 50 \Omega$; $R_2 = 45 \Omega$; $R_3 = 40 \Omega$; $R_4 = 55 \Omega$; $R_5 = 60 \Omega$;
 $U = 48 \text{ V}$;

Ges.: $J_x = ?$

Lös.:



R_1 u. R_2 u. R_3
liegen parallel!



$$R_a = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}} = \frac{1}{\frac{1}{50} + \frac{1}{45} + \frac{1}{40}} \Omega = \underline{\underline{14,9 \Omega}}$$

Spannungsteiler:

$$\frac{U_a}{U} = \frac{R_a}{R_4 + R_a} \sim U_a = U \cdot \frac{R_a}{R_4 + R_a} = 48 \text{ V} \cdot \frac{14,9 \Omega}{55 \Omega + 14,9 \Omega} = \underline{\underline{10,2 \text{ V}}}$$

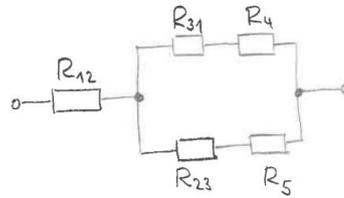
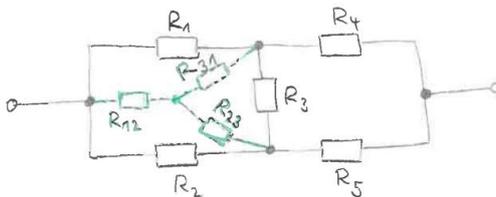
$$\underline{\underline{J_x}} = J_2 + J_5 = \frac{U_a}{R_2} + \frac{U}{R_5} = \frac{10,2 \text{ V}}{45 \frac{\text{V}}{\text{A}}} + \frac{48 \text{ V}}{60 \frac{\text{V}}{\text{A}}} = \underline{\underline{1,03 \text{ A}}}$$

Aufgabe 2.7

Geg.: $R_1 = 55 \Omega$; $R_2 = 40 \Omega$; $R_3 = 45 \Omega$; $R_4 = 40 \Omega$; $R_5 = 60 \Omega$;

Ges.: Ersatzwiderstand R ?

Lös.:



Stern-Dreieck-Umwandlung:

$$R_{12} = \frac{R_1 R_2}{R_1 + R_2 + R_3} = \frac{55 \Omega \cdot 40 \Omega}{55 \Omega + 40 \Omega + 45 \Omega} = 15,7 \Omega ;$$

$$R_{23} = \frac{R_2 R_3}{R_1 + R_2 + R_3} = \frac{40 \Omega \cdot 45 \Omega}{55 \Omega + 40 \Omega + 45 \Omega} = 12,9 \Omega ;$$

$$R_{31} = \frac{R_3 R_1}{R_1 + R_2 + R_3} = \frac{45 \Omega \cdot 55 \Omega}{55 \Omega + 40 \Omega + 45 \Omega} = 17,7 \Omega ;$$

$$\underline{\underline{R}} = R_{12} \cdot \frac{(R_{31} + R_4) \cdot (R_{23} + R_5)}{(R_{31} + R_4) + (R_{23} + R_5)} =$$

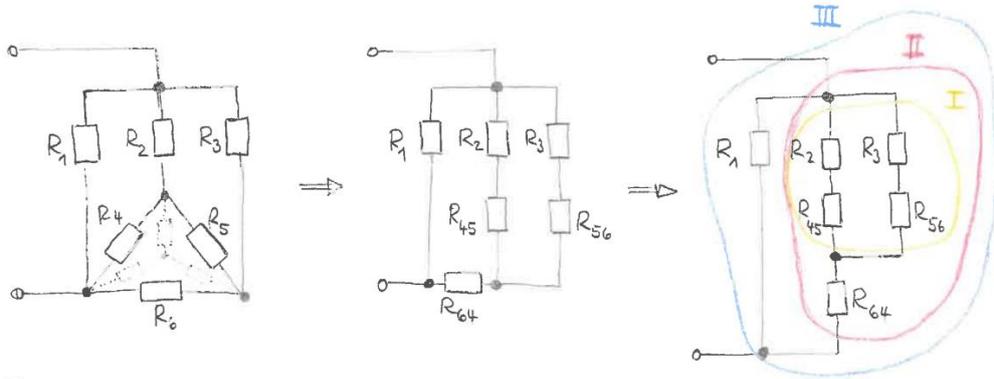
$$= 15,7 \Omega \cdot \frac{(17,7 \Omega + 40 \Omega) \cdot (12,9 \Omega + 60 \Omega)}{17,7 \Omega + 40 \Omega + 12,9 \Omega + 60 \Omega} = \underline{\underline{50,8 \Omega}} ;$$

Aufgabe 2.8

Geg.: $R_1 = 1,0 \text{ k}\Omega$; $R_2 = 1,5 \text{ k}\Omega$; $R_3 = 2,0 \text{ k}\Omega$;
 $R_4 = 3,0 \text{ k}\Omega$; $R_5 = 2,0 \text{ k}\Omega$; $R_6 = 2,5 \text{ k}\Omega$;

Ges.: Ersatzwiderstand R ?

Lös.:



$$R_{45} = \frac{R_4 R_5}{R_4 + R_5 + R_6} = \frac{3,0 \text{ k}\Omega \cdot 2,0 \text{ k}\Omega}{3,0 \text{ k}\Omega + 2,0 \text{ k}\Omega + 2,5 \text{ k}\Omega} = 0,8 \text{ k}\Omega;$$

$$R_{56} = \frac{R_5 R_6}{R_4 + R_5 + R_6} = \frac{2,0 \text{ k}\Omega \cdot 2,5 \text{ k}\Omega}{3,0 \text{ k}\Omega + 2,0 \text{ k}\Omega + 2,5 \text{ k}\Omega} = 0,67 \text{ k}\Omega;$$

$$R_{64} = \frac{R_6 R_4}{R_4 + R_5 + R_6} = \frac{2,5 \text{ k}\Omega \cdot 3,0 \text{ k}\Omega}{3,0 \text{ k}\Omega + 2,0 \text{ k}\Omega + 2,5 \text{ k}\Omega} = 1,0 \text{ k}\Omega;$$

$$\text{I.) } R_{\text{I}} = \frac{(R_2 + R_{45}) \cdot (R_3 + R_{56})}{R_2 + R_{45} + R_3 + R_{56}} = \frac{(1,5 \text{ k}\Omega + 0,8 \text{ k}\Omega) \cdot (2,0 \text{ k}\Omega + 0,67 \text{ k}\Omega)}{1,5 \text{ k}\Omega + 0,8 \text{ k}\Omega + 2,0 \text{ k}\Omega + 0,67 \text{ k}\Omega} = 1,235 \text{ k}\Omega;$$

$$\text{II.) } R_{\text{II}} = R_{\text{I}} + R_{64} = 1,235 \text{ k}\Omega + 1,0 \text{ k}\Omega = 2,235 \text{ k}\Omega;$$

$$\text{III.) } R_{\text{III}} = \frac{R_1 \cdot R_{\text{II}}}{R_1 + R_{\text{II}}} = \frac{1,0 \text{ k}\Omega \cdot 2,235 \text{ k}\Omega}{1,0 \text{ k}\Omega + 2,235 \text{ k}\Omega} = 0,691 \text{ k}\Omega = 691 \Omega;$$

$$\Rightarrow R = R_{\text{III}} = 691 \Omega;$$